# SOCI 320-500 <br> Demographic Methods <br> Fall 2019 

## ASSIGNMENT 3

# Due by November 24, 2019 (Sunday) at 11:59pm <br> Maximum of possible points: 20 

## Instructor information

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## Purpose

The purpose of this assignment is to test the knowledge about topics on population projection, period fertility, and age pyramids, as discussed in the classroom and in the textbook (Wachter, Kenneth W. 2014. Essential Demographic Methods. Cambridge: Harvard University Press).

## Task

The following questions are related to demographic concepts and methods. Answers to substantive questions should be no more than 150 words and written in Microsoft Word. The Word document should be on US Letter paper size, one-inch margins, Arial font, size 11, 1.5 line spacing. Answers to methods questions should be solved in Microsoft Excel, but the final results and interpretations should be exported and properly formatted in the Word document. Look at examples of how to properly format tables and figures in Word at http://www.ernestoamaral.com/docs/soci320-19fall/Examples_tab_fig.pdf.

Questions 5.3 and 10.1 are worth 4 points each. All other questions are worth 2 points each.

## Submission

Students must email the Excel file to the professor. The Word file should be submitted through Turnitin within eCampus. Turnitin is an online database system designed to help instructors detect plagiarism, track citations, facilitate peer reviews, and provide paperless grading markup in written assignments. Students should develop this assignment individually.

## Questions - Chapter 5 - Population projection

5.1. Using lifetable person-years lived entries for the cohort of U.S. women born in 1934 from Table 4.2, calculate subdiagonal entries for a Leslie matrix with 5 -year-wide ( $n=5$ ) age groups. Assume $10=1,000$, $f_{\text {fab }}=0.4877,5 f_{50}=0$ and $5 L 50=4,421$.

Table 4.2 A cohort $N R R$ from U.S. age-specific rates

| age-specific rates |  |  |  |
| ---: | :---: | :---: | ---: |
| $x$ | ${ }_{5} f_{x}$ | ${ }_{5} L_{x}$ | Babies |
| 0 | 0 | 4770 | 0 |
| 5 | 0 | 4726 | 0 |
| 10 | 0 | 4712 | 0 |
| 15 | 0.0811 | 4698 | 381 |
| 20 | 0.2384 | 4681 | 1116 |
| 25 | 0.1969 | 4662 | 918 |
| 30 | 0.1033 | 4637 | 479 |
| 35 | 0.0313 | 4604 | 144 |
| 40 | 0.0046 | 4561 | 21 |
| 45 | 0.0009 | 4503 | 4 |
|  |  |  | 3,063 |

5.2. Using age-specific fertility rates for the cohort of U.S. women born in 1934 from Table 4.2, calculate entries in the first row of a Leslie matrix with 5 -year-wide ( $n=5$ ) age groups.
5.3. The matrix $A$ shown below is a Leslie matrix for projecting the female population of Argentina. There are three age groups, each 18 years wide. The starting population for 1992 includes 3.9 million girls aged 0 to $18,3.3$. million women aged 18 to 36 , and 2.8 million women aged 36 to 54.

$$
A=\left(\begin{array}{ccc}
0.551 & 0.556 & 0.037 \\
0.962 & 0 & 0 \\
0 & 0.909 & 0
\end{array}\right)
$$

(a) How long is the interval of time covered by a single projection step?
(b) What is the total population of women up to age 54 after one projection step?
(c) What is the total population of women up to age 54 after three projection steps? To what year would this total apply?
(d) At what rate would the population of Argentina be growing according to this projection over three projection steps?

## Questions - Chapter 6 - Period fertility

6.1. Calculate the period TFR, GRR, NRR and synthetic cohort mean age at childbearing $\mu$ from data in Table 6.7 for women in the African country of Togo in 1961 from Keyfitz and Flieger (1968). It is rare to have such data from Africa from the 1960s, epitomizing high mortality and fertility unaffected by fertility decline. The period lifetable radix is 100,000 , the total female population is 813,295 , and 41,315 babies in 1961 were boys and 42,855 were girls.

Table 6.7 Period data for women in Togo for 1961

| $\boldsymbol{x}$ | ${ }_{n} B_{x}$ | ${ }_{n} D_{x}$ | ${ }_{n} K_{x}$ | ${ }_{n} L_{x}$ |
| :--- | ---: | ---: | ---: | :---: |
| 15 | 7,150 | 578 | 48,564 | 337,775 |
| 20 | 21,910 | 502 | 67,096 | 321,570 |
| 25 | 25,305 | 1,034 | 80,746 | 306,003 |
| 30 | 14,825 | 659 | 53,670 | 287,031 |
| 35 | 9,935 | 638 | 51,975 | 270,049 |
| 40 | 3,625 | 441 | 32,022 | 253,276 |
| 45 | 1,420 | 638 | 32,307 | 232,925 |

Source: Keyfitz and Flieger (1968, pp. 74-75).
6.2. Taking the population counts from Table 6.3 as a standard, calculate an age-standardized birth rate for Togo in 1961. Calculate an age-standardized birth rate for the Hutterites using the rates in Table 6.4. Compare the two answers.

Table 6.3 An age-standardized birth rate

|  |  |  | Standard <br>  <br> $x$ | France <br> ${ }_{n} K_{x}$ | Product <br> (babies) |
| :--- | ---: | ---: | :---: | :---: | :---: |
|  | 0 | 15 | 882 | 0 | 0 |
| W | 15 | 5 | 270 | 0.008 | 2.107 |
| O | 20 | 5 | 248 | 0.056 | 13.864 |
| M | 25 | 5 | 245 | 0.134 | 32.726 |
| E | 30 | 5 | 232 | 0.118 | 27.483 |
| N | 35 | 5 | 209 | 0.050 | 10.531 |
|  | 40 | 5 | 182 | 0.012 | 2.108 |
|  | 45 | 5 | 164 | 0.000 | 0 |
|  | 50 | $\infty$ | 574 | 0 | 0 |
| M |  |  |  |  |  |
| E | 0 | $\infty$ | 3,051 | 0 | 0 |
| N |  |  |  |  |  |

Source: United Nations World Population Prospects (2001).

| Table 6.4 | Calculating $I_{\mathrm{f}}$ and $I_{\mathrm{g}}$ for Berlin in 1900 |  |  |  |  |
| :--- | :---: | ---: | ---: | ---: | ---: |
|  | Hutterite | Overall | Implied | Married | Implied |
| Age $x$ | Rates | Women | Babies | Women | Babies |
| 15 | 0.300 | 91,358 | 27,407 | 1,538 | 461 |
| 20 | 0.550 | 114,464 | 62,955 | 28,710 | 15,791 |
| 25 | 0.502 | 99,644 | 50,021 | 55,417 | 27,819 |
| 30 | 0.407 | 88,886 | 36,177 | 62,076 | 25,265 |
| 35 | 0.406 | 75,729 | 30,746 | 55,293 | 22,449 |
| 40 | 0.222 | 66,448 | 14,751 | 47,197 | 10,478 |
| 45 | 0.061 | 54,485 | 3,324 | 36,906 | 2,251 |
| Sum |  | 591,014 | 225,381 | 287,137 | 104,514 |

6.3. Period TFR's in France were 1.746 in 1995 to 2000, 1.878 in 2000 to 2005, and 1.968 in 2005 to 2010 according to the HFD. Average ages at childbirth based on period ${ }_{n} F_{x}$ values were $A(1995)=28.98$, $A(2000)=29.38, A(2005)=29.71$, and $A(2010)=30.03$. Compute values of $T F R(\mathrm{~s})$ standardized for birth age for each period and compare these tempo-adjusted values to the original period TFR's.
6.4. About 126 million babies were born into the world in the year 2000. Calculate a value of the Princeton Index $I f$ for the whole world based on population counts by age in Table 6.3. Hypothetical proportions married in 5 -year age groups from 15 upward were $0.20,0.70,0.85,0.90,0.94,0.92$, and 0.90 , and, at a rough guess, perhaps $90 \%$ of these births were within marriage. Calculate implied values of $I_{\mathrm{g}}$ and $I_{\mathrm{m}}$. How close is $I_{\mathrm{f}}$ to the product of $I_{\mathrm{g}}$ and $I_{\mathrm{m}}$ ?

## Question - Chapter 10.1 - Age pyramids

10.1. Select two U.S. states and collect data to create bar graphs with age-sex structure for 2010 and 2017 (see example in Figure 1). Estimate child dependency ratio, old-age dependency ratio, and total dependency ratio for each state in each year. Use data from the American Community Survey (ACS) fiveyear estimates, which are available in the "Tables" tool within the U.S. Census Bureau data website (https://data.census.gov/). Include graphs with age-sex structure and table with dependency ratios in your report and analyze them.

Figure 1. Age-sex structure of Brazilian population, 1970 and 2000


Source: 1970 and 2000 Brazilian Demographic Censuses.

