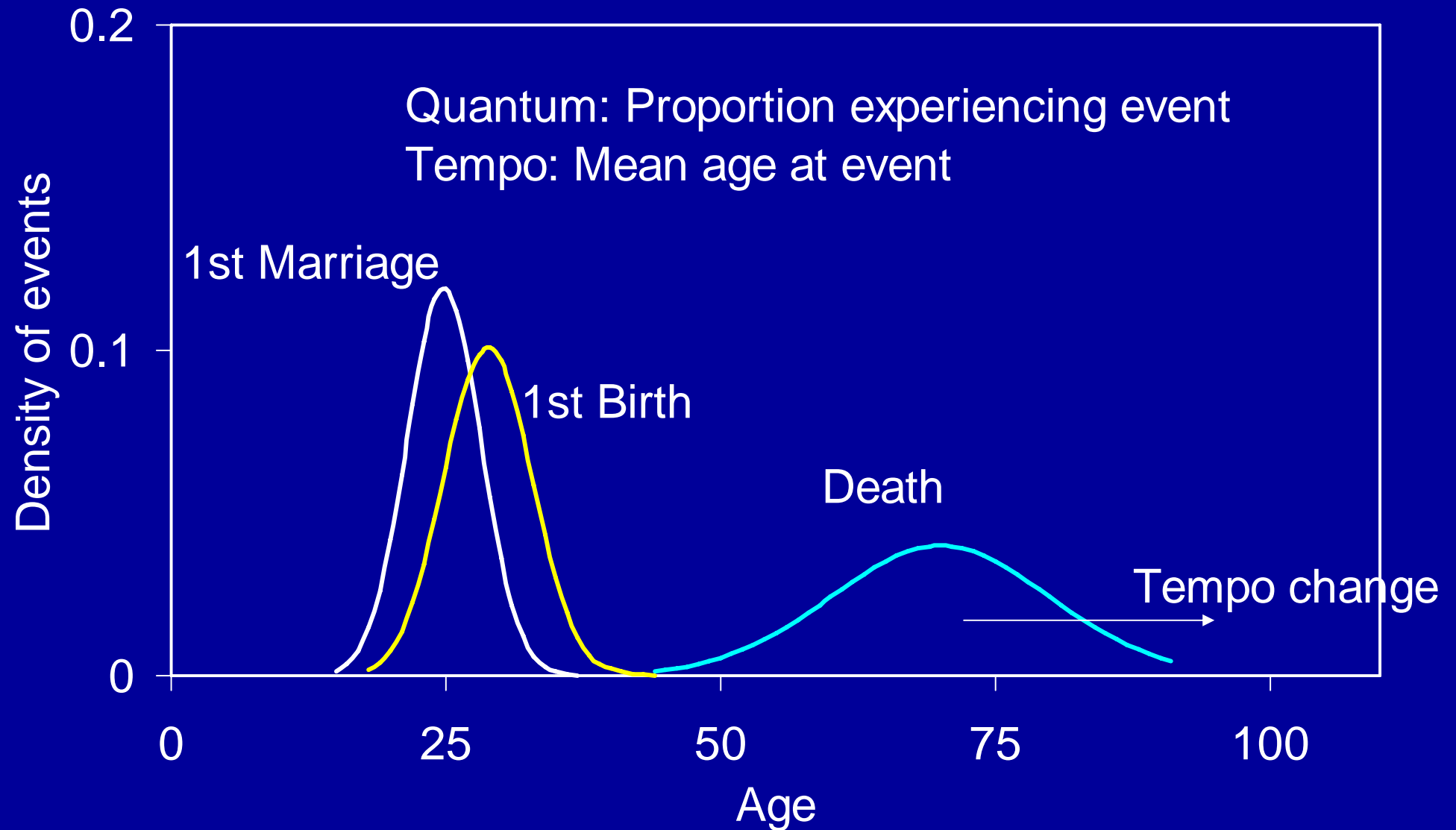


# The quantum and tempo of life cycle events

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Population Council

## Distribution of life cycle events by age



## Period measures of quantum and tempo (2<sup>nd</sup> kind)

	QUANTUM	TEMPO
Birth	Total fertility rate <i>TFR(t)</i>	Mean age at birth <i>MAB(t)</i>
Marriage	Total marriage rate <i>TNR(t)</i>	Mean age at marriage <i>MAM(t)</i>
Death	Total mortality rate <i>TMR(t)</i>	Mean age at death <i>MAD(t)</i>

a. Tempo distortions in the  
total fertility rate

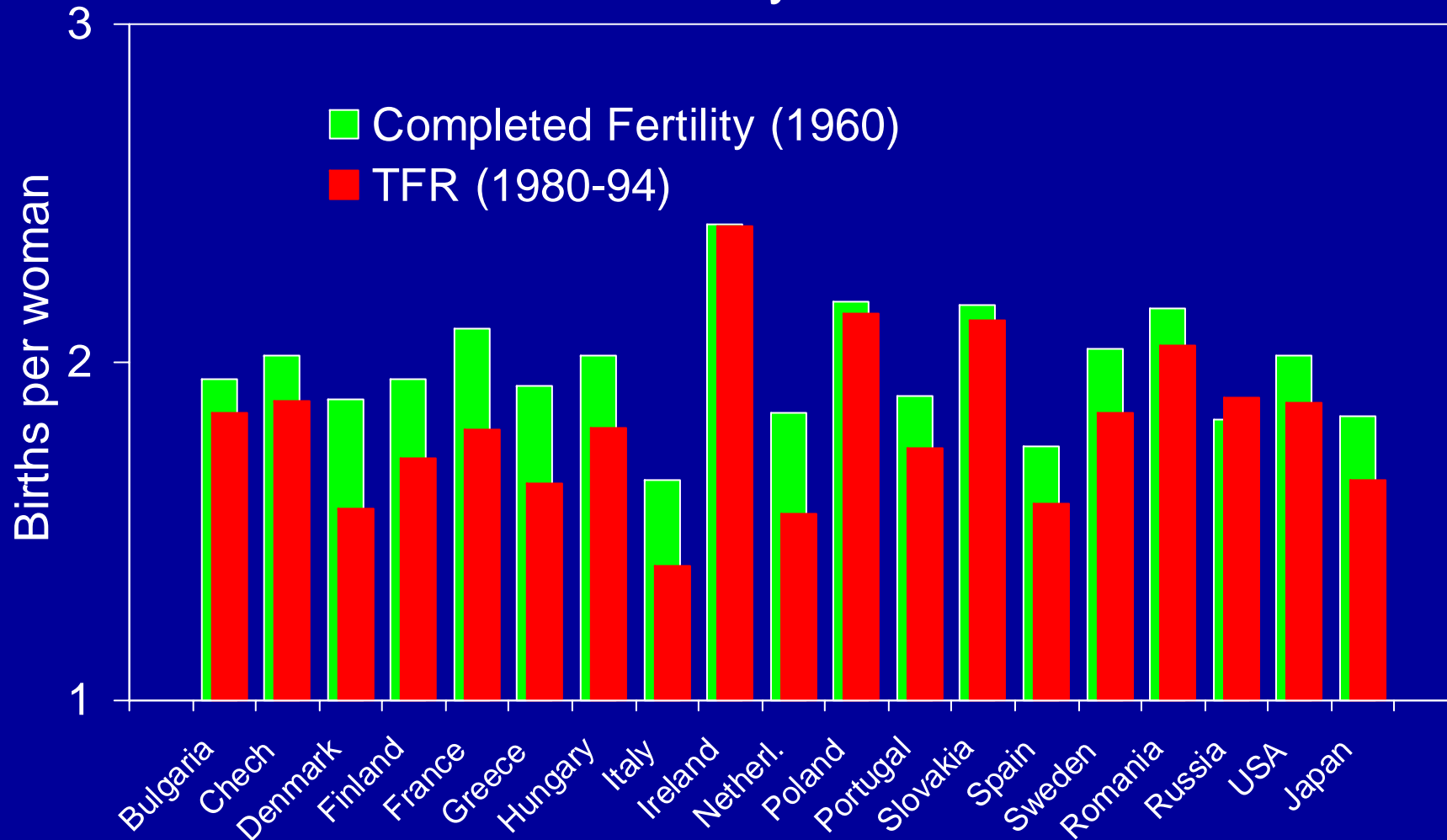
## Total fertility rate, France 1975-2000

Period	TFR (births per woman)
1975-80	1.86
1980-85	1.87
1985-90	1.81
1990-95	1.71
1995-00	1.73
Average 1975-2000	1.80
Completed fertility of 1960 cohort	?

## Total fertility rate, France 1975-2000

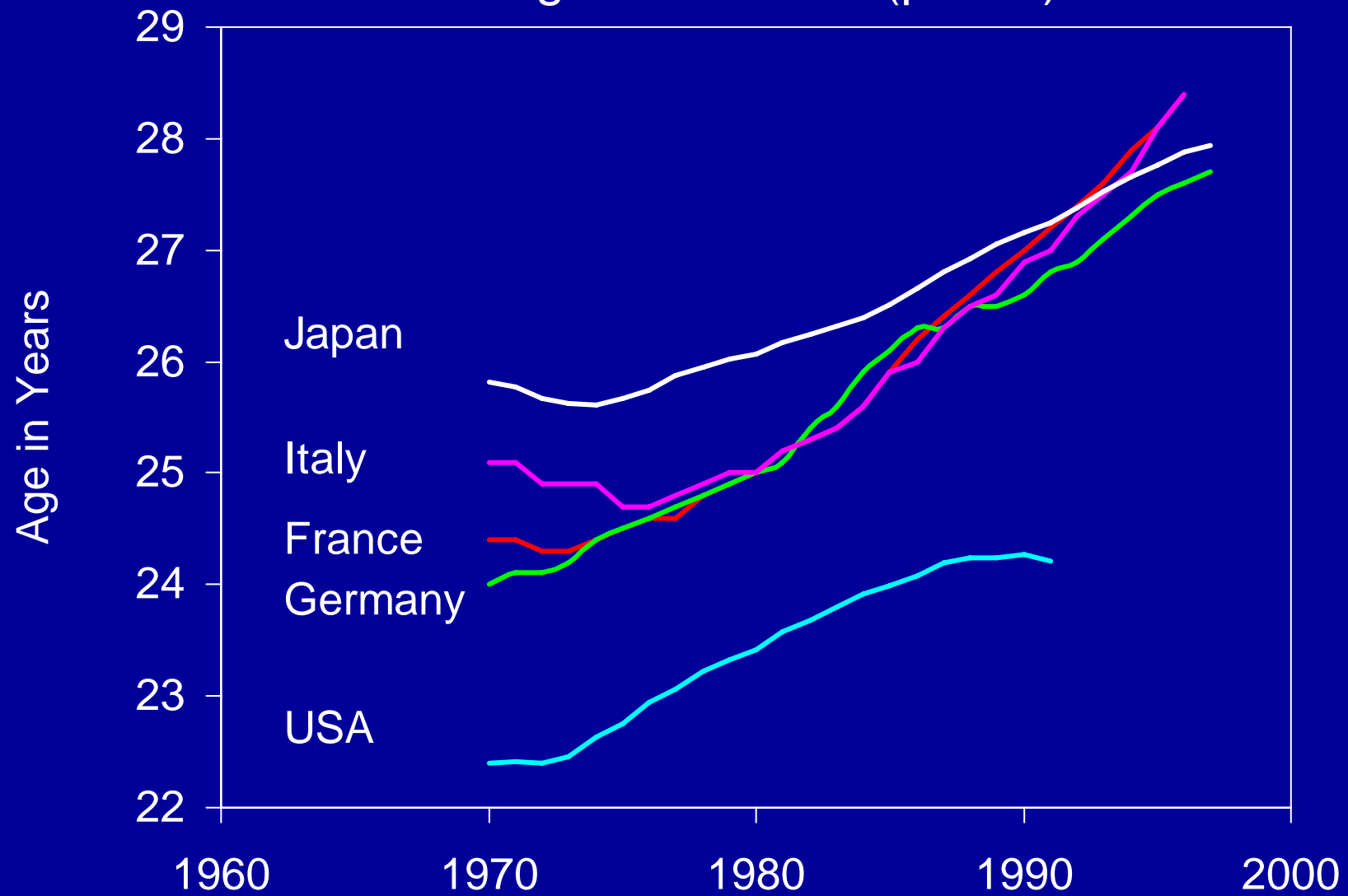
Period	Observed TFR	Undistorted TFR
1975-80	1.86	?
1980-85	1.87	?
1985-90	1.81	?
1990-95	1.71	?
1995-00	1.73	?
Average 1975-2000	1.80	?
Completed fertility 1960 cohort	2.10	

## Completed fertility (1960 cohort) and total fertility rate 1980-94



Source: UN 1999, Council of Europe 2000

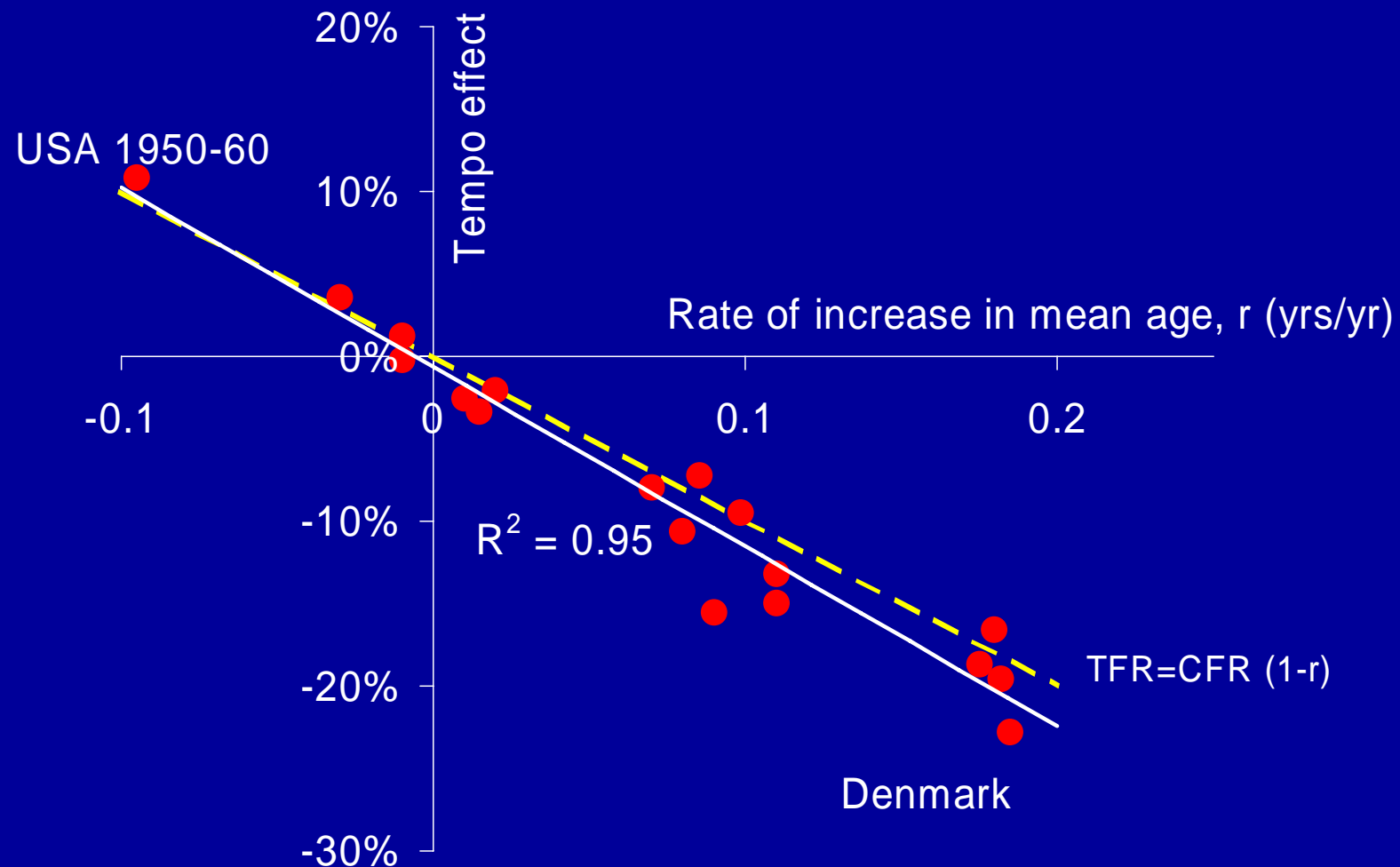
## Mean age at first birth (period)



Source: Council of Europe 2000



# Tempo effect (TFR/CFR-1) at birth order one by increase in mean age at first birth, 1980-90



# Correction of tempo distortion

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Tempo adjusted TFR:

$$TFR^*(t) = \frac{TFR(t)}{1 - r(t)}$$

$$r(t) = \frac{dMAB(t)}{dt}$$

## Fertility in France

TFR (1980-1995) = 1.80

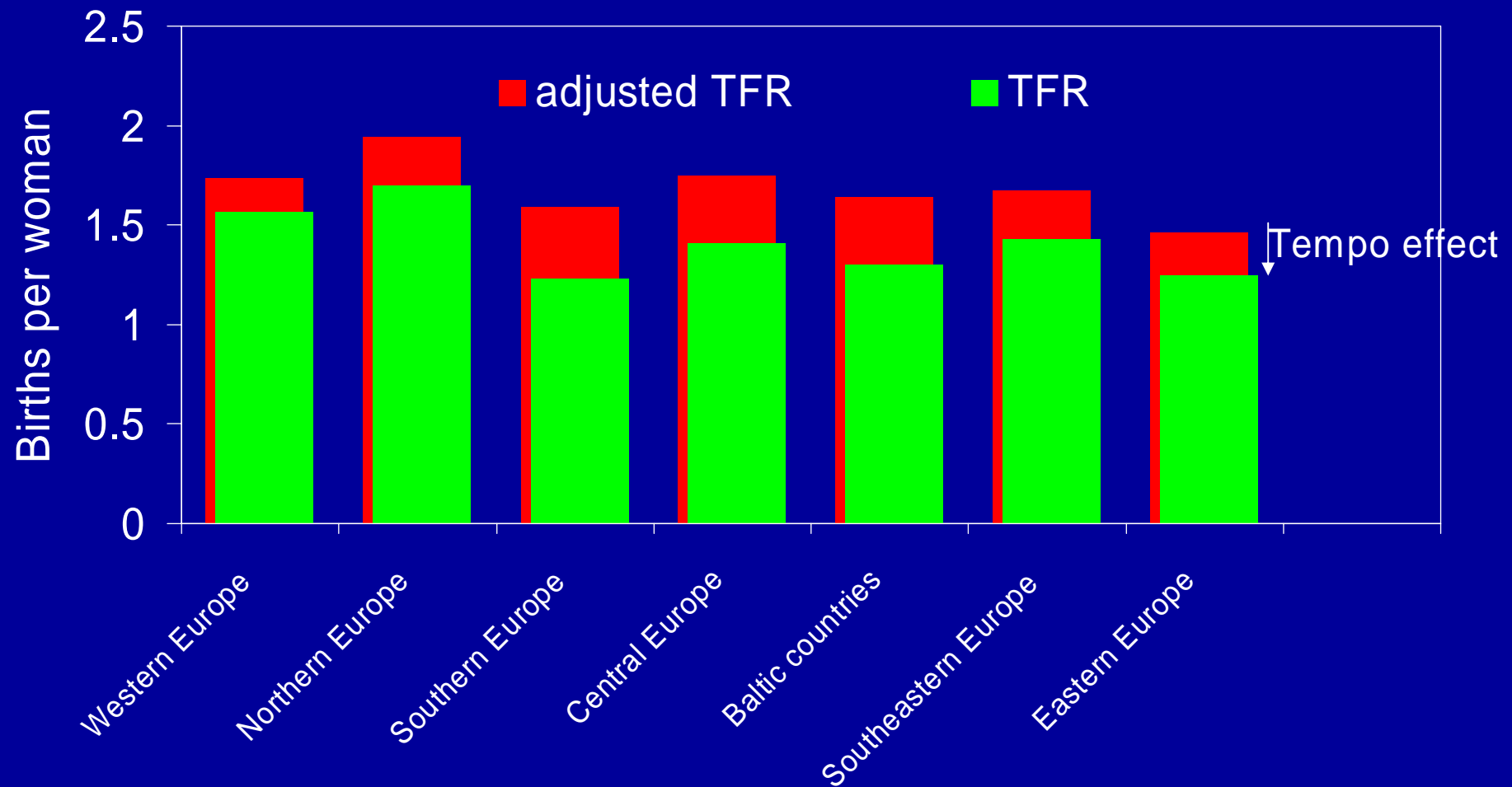
Cohort fertility (1960) = 2.10

Rate of increase in mean age (r) = 0.15/year

Distortion index (1-r)=0.85

Tempo adjusted TFR\* =  $1.8 / 0.85 = 2.11$

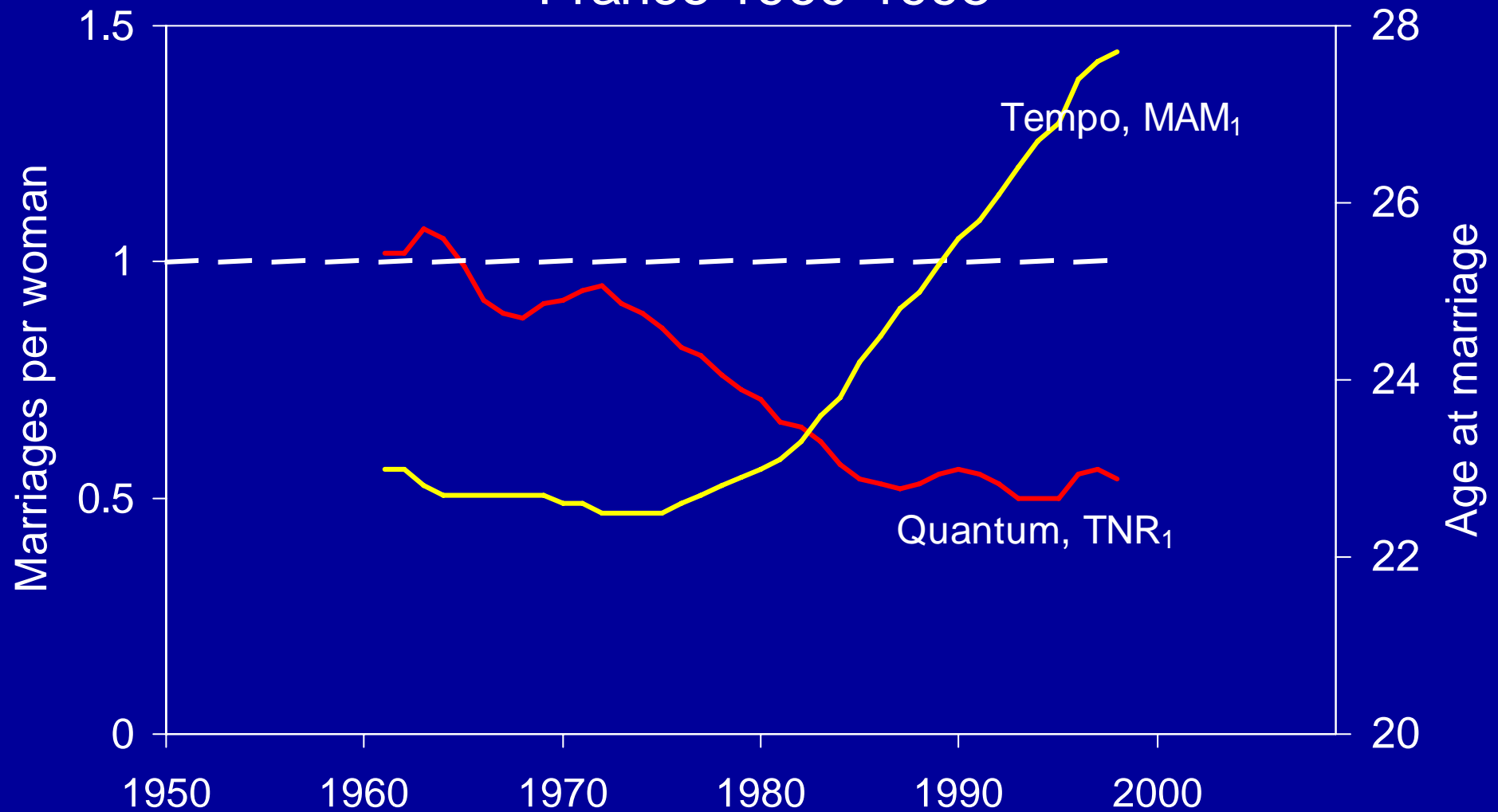
# Total fertility rate with and without the tempo effect 1995-2000



Source: Sobotka 2004

b. Tempo distortions in the  
total marriage rate

## Quantum and tempo of first marriage, France 1960-1998



## Removing tempo distortion in total marriage rate

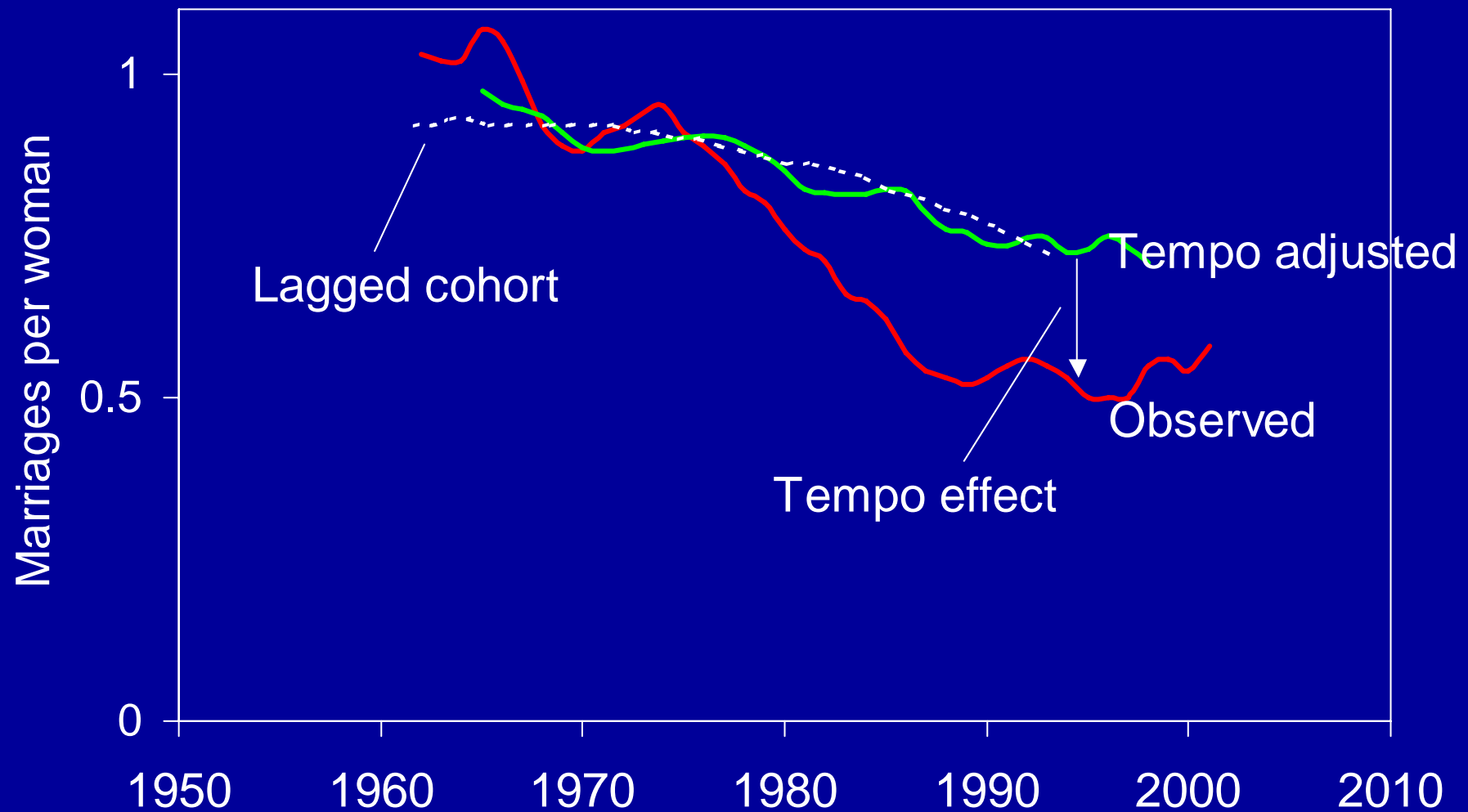
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Tempo adjusted *TNR*:

$$TNR^*(t) = \frac{TNR(t)}{1 - r(t)}$$

$$r(t) = \frac{dMAM(t)}{dt}$$

## Total first marriage rate, observed and adjusted, France





c. Tempo distortions in the  
total mortality rate

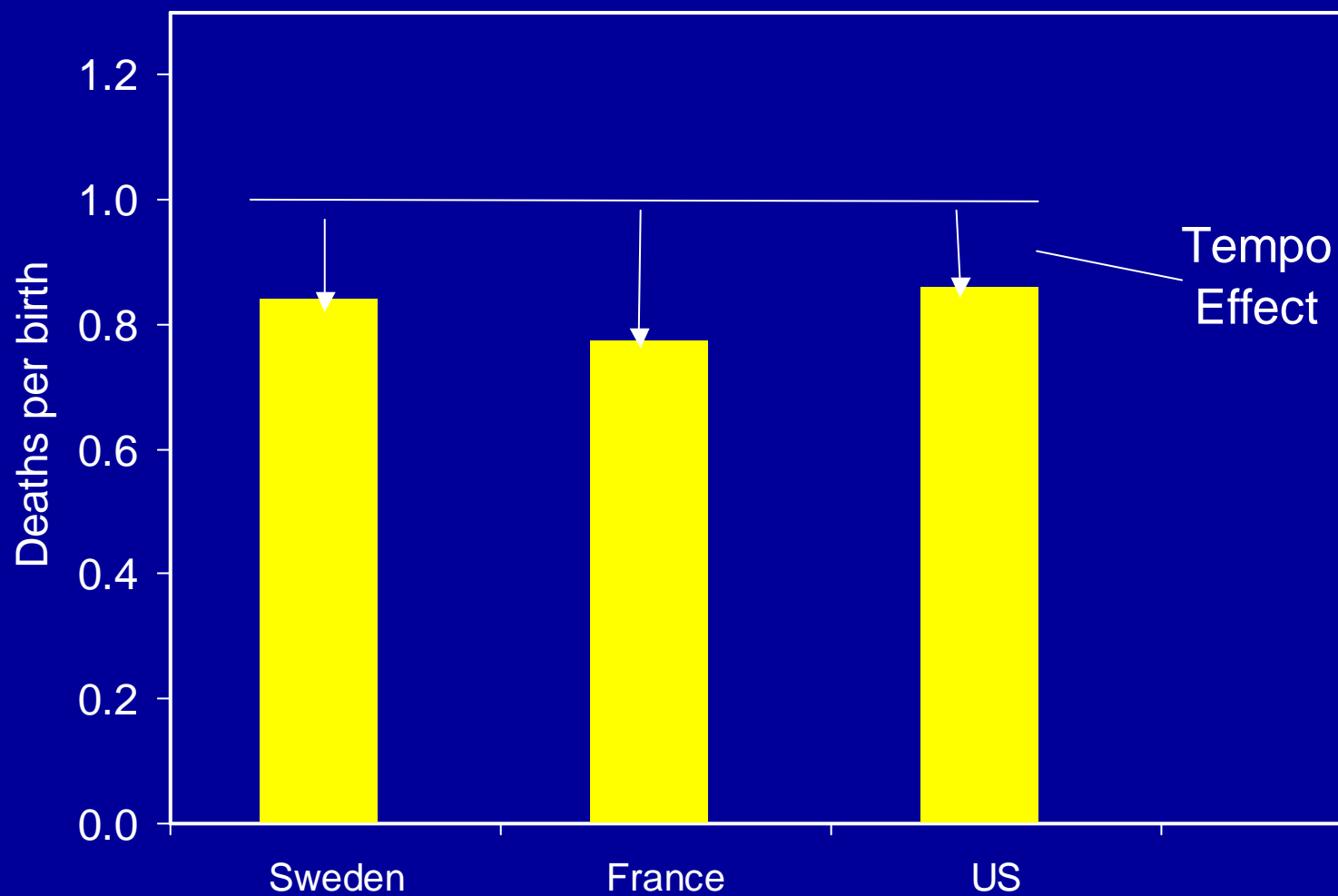
Age specific death rates of 2<sup>nd</sup> kind

$$d(a, t) = \frac{\text{death at age } a \text{ and time } t}{\text{Persons born at time } t - a}$$

Total mortality rate

$$TMR(t) = \int_0^{\infty} d(a, t) da = \int_0^{\infty} \mu(a, t) l_c(a, t - a) da$$

## Total mortality rate, females, average 1980-95



Note: No mortality under age 30

## Removing tempo distortion

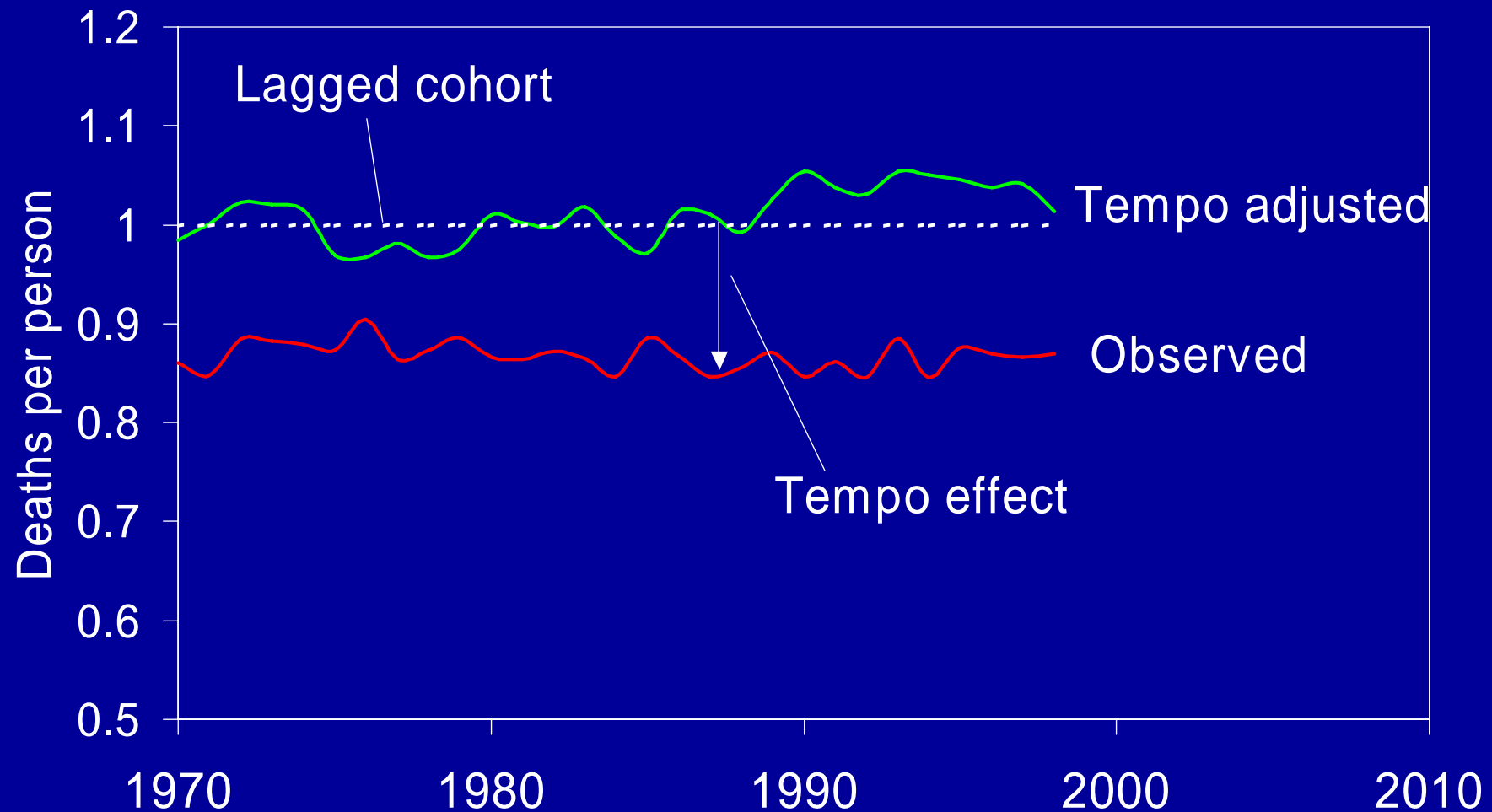
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Tempo adjusted Total Mortality Rate:

$$TMR^*(t) = \frac{TMR(t)}{1 - r(t)} = 1$$

$$r(t) = dMAD(t) / dt$$

# Total mortality rate, observed and adjusted, England and Wales



Tempo distortions in the  
tempo measures of 2<sup>nd</sup> kind

# Tempo measures, adjusted and unadjusted

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Mean age at birth

$$MAB(t) = \int_0^{\infty} a \frac{f(a,t)}{TFR(t)} da = MAB^*(t)$$

Mean age at marriage

$$MAM(t) = \int_0^{\infty} a \frac{n(a,t)}{TNR(t)} da = MAM^*(t)$$

Mean age at death

$$MAD(t) = \int_0^{\infty} a \frac{m(a,t)}{TMR(t)} da = MAD^*(t)$$

## Conclusions on tempo distortions in measures of the 2<sup>nd</sup> kind

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Quantum measures: Distorted, but can be adjusted

Tempo measures: Not distorted

Assumption: Invariant shape of age pattern of rates



## II. Tempo distortions in period measures of 1<sup>st</sup> kind

# Rates of demographic events

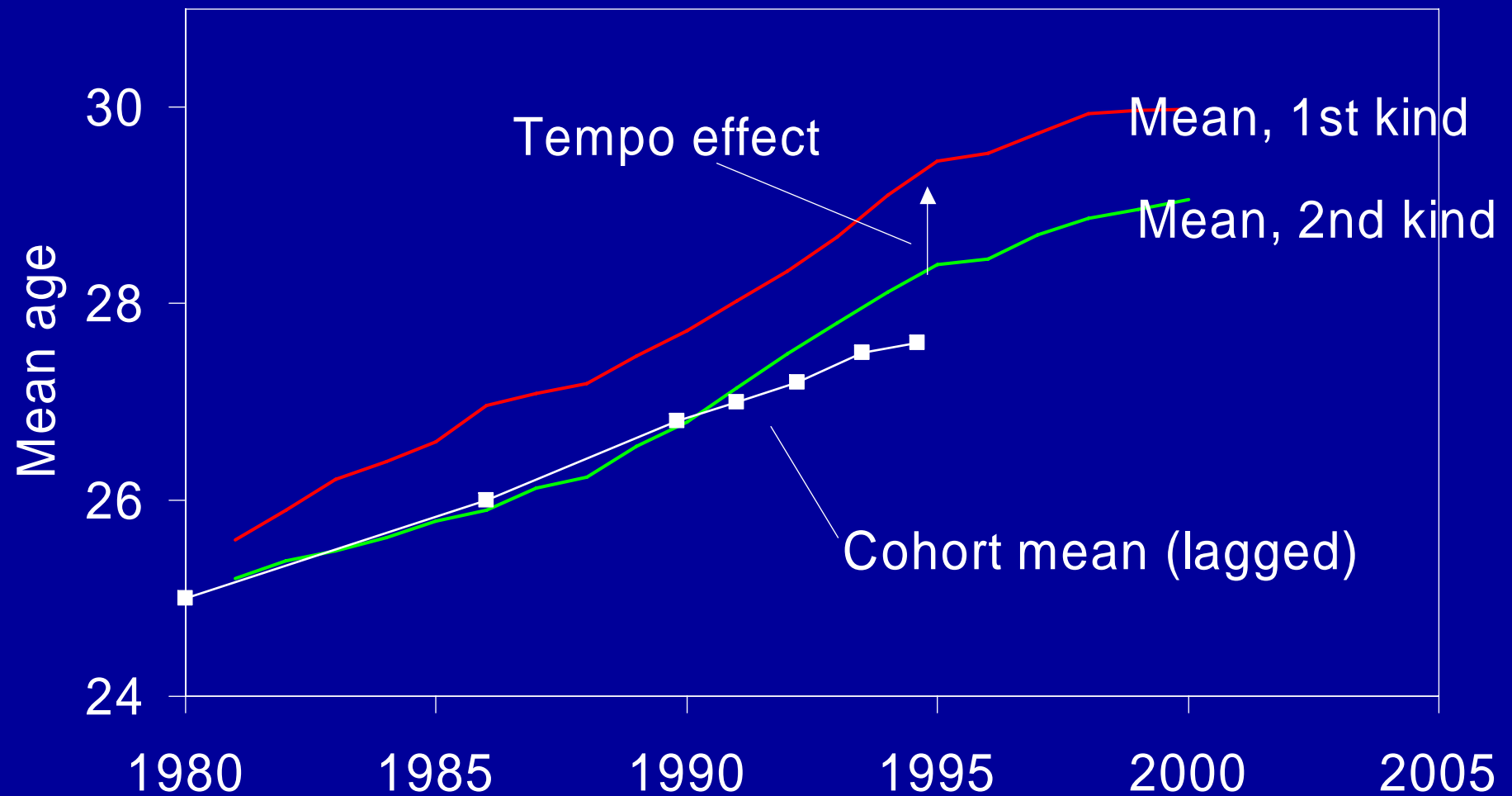
<u>Rate of the 1st kind</u>	<u>Rate of 2<sup>nd</sup> kind</u>
<ul style="list-style-type: none"><li>- Conditional rate</li><li>- Probability</li><li>- Intensity</li><li>- Hazard</li><li>- Risk</li><li>- Occurrence/exposure</li></ul>	<ul style="list-style-type: none"><li>- Unconditional rate</li><li>- Frequency</li><li>- Incidence</li><li>- Density</li></ul>
Example: Force of mortality	Example: Conventional age specific birth/marriage rate
Used in life tables, e.g. to estimate period life expectancy	Used to calculate quantum measures such as total fertility rate

# Period measures of quantum and tempo (1st kind)

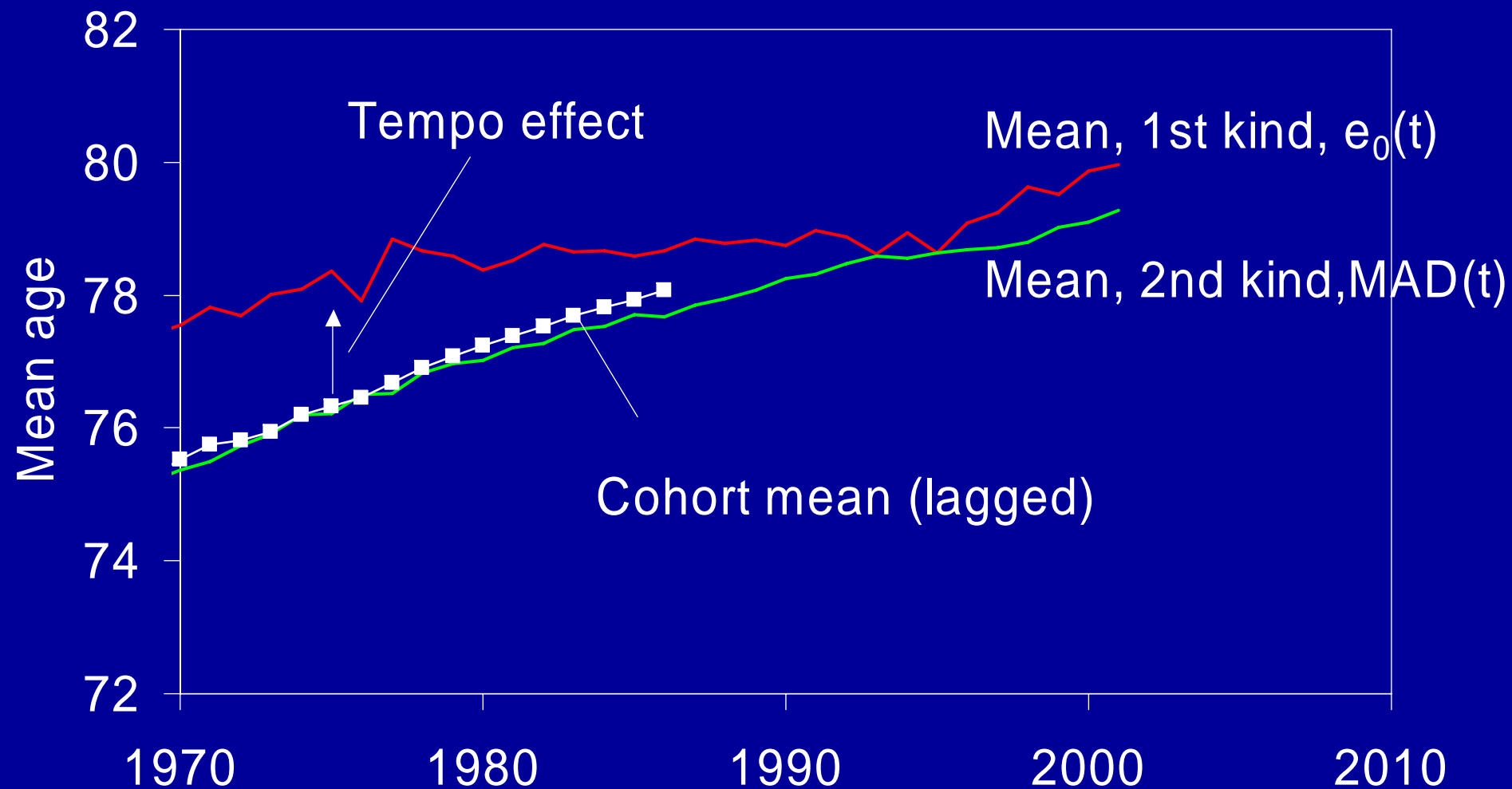
## Life table estimates

	QUANTUM	TEMPO
Birth (1st)	Proportion ever had 1 <sup>st</sup> birth: $TFR_L(t)$	Mean age at 1 <sup>st</sup> birth: $MAB_L(t)$
Marriage (1st)	Proportion ever married: $TNR_L(t)$	Mean age at 1 <sup>st</sup> marriage: $MAM_L(t)$
Death	Proportion ever dying: $TMR_L(t)=1$	Mean age at death: $MAD_L(t)$ =life expectancy, $e_0(t)$

Mean age at first birth of first and second kind  
and lagged cohort mean. Spanish females.



Mean age at death of first and second kind  
and lagged cohort mean. Danish females.



# Correcting for tempo distortions in tempo measures of 1<sup>st</sup> kind

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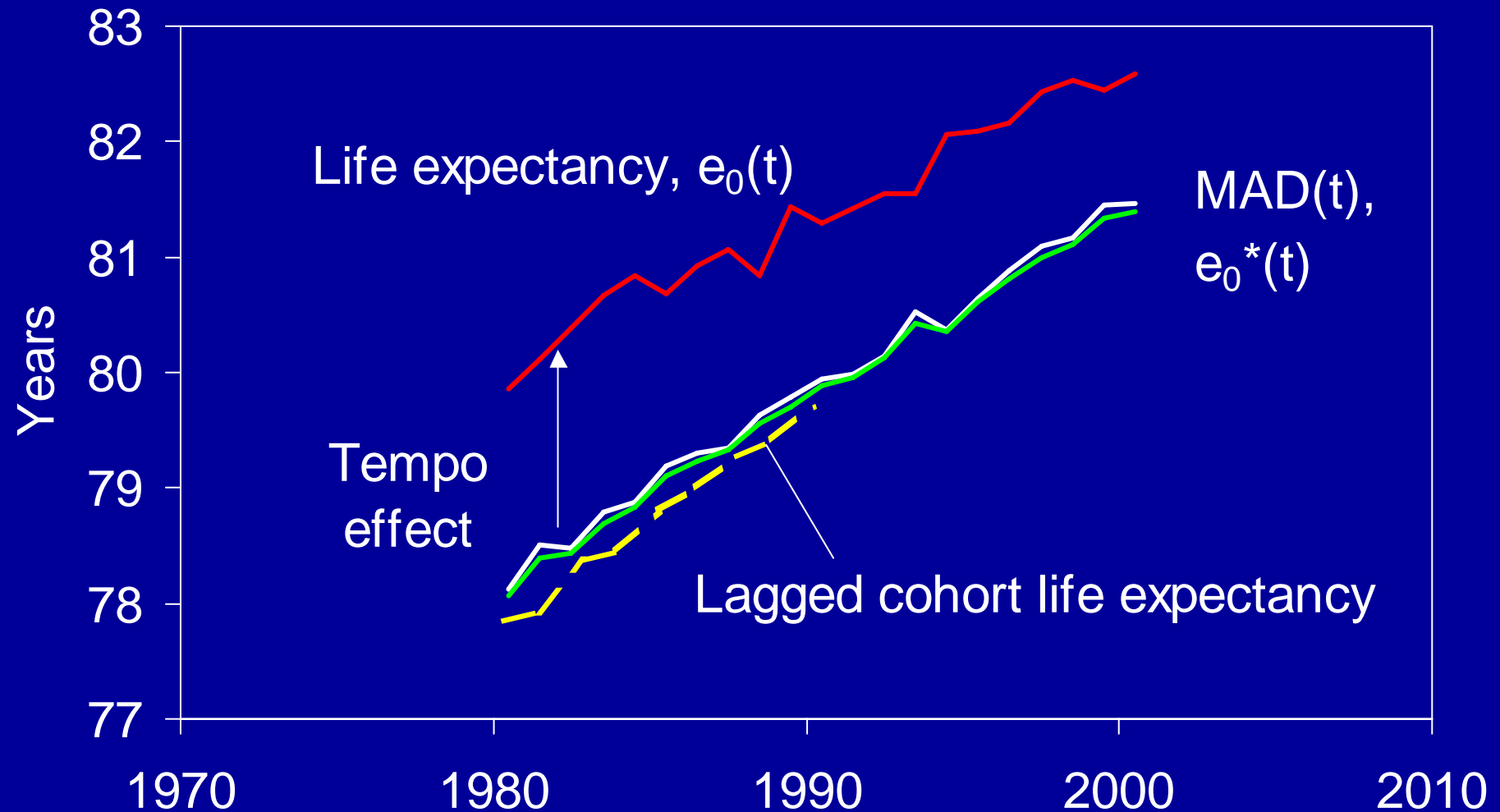
Life expectancy/ mean age at death of 1<sup>st</sup> kind

$$e_0(t) = \int_0^{\infty} \exp\left[-\int_0^x \mu(a, t) da\right] dx$$

Tempo adjusted life expectancy

$$e_0^*(t) = \int_0^{\infty} \exp\left[-\int_0^x \frac{\mu(a, t)}{1 - r(t)} da\right] dx$$

# Trends in alternative mortality tempo measures, Swedish females, 1980-2000 (no mortality under age 30)



## Evidence for tempo distortion of period tempo measures of 1<sup>st</sup> kind

- 1) Theoretical argument
- 2) Difference between means of 1<sup>st</sup> and 2<sup>nd</sup> kind
- 3) Difference disappears when mean stalls
- 4) Lagged cohort mean equals mean of 2<sup>nd</sup> kind
- 5) Tempo adjustment removes difference



## Conclusions

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- Standard methods for measuring period quantum and tempo apply to all life-cycle events
- Period quantum measures of 2<sup>nd</sup> kind are distorted by tempo effects
- Life table estimates of period quantum and tempo are distorted
- Distortions can be removed with BF procedure for rates of 1<sup>st</sup> and 2<sup>nd</sup> kind (assuming constant shape)

